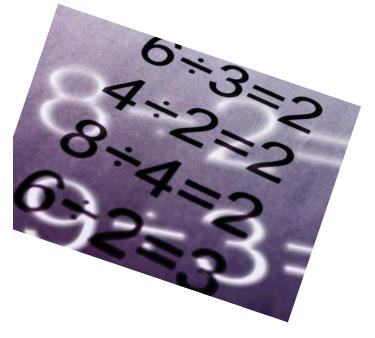
Critical Foundations for Algebra





Group Norms

Listening: SLANT

Cell phone reminder

Conversations

Breaks



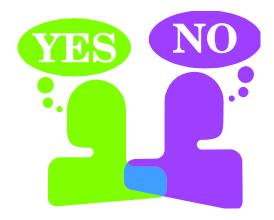
Bathroom location



Response Cards

Purpose

Critical Foundations for Algebra poll



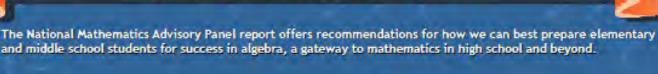
National Mathematics Advisory Panel Report



Doing What Works
Resources are based
on the
recommendations of
the National
Mathematics Advisory
Panel

The National Mathematics Advisory Panel conducted a systematic and rigorous review of the best available scientific evidence for the teaching and learning of mathematics and provided recommendations that lay out concrete steps to improve mathematics education, with a specific focus on preparation for learning algebra.





Mathematics Preparation for Algebra

- -Follow a focused, coherent progression of mathematics
- Achieve proficiency with whole numbers, fractions, and aspects of geometry and measurement
- -Build deep understanding
- -Emphasize fractions and related concepts

AA-1

Comprehensive Instruction

- Develop conceptual understanding, computational fluency, and problem-solving skills
- -Achieve automaticity in computation
- -Provide adequate practice
- -Encourage effort and persistence



Mastery Framework

- -Set benchmarks for key skills
- -Use formative assessments
- -Provide explicit instruction for struggling students
- -Offer acceleration and enrichment for gifted students



Grade-Level Benchmarks for Critical Foundations* 15T

	Terror.			a service	and the same
3RD	Add	and sub	tract w	vhole	numbers

4TH	8	Identify	represent,	ond	compare	fractions	and	decimals
-		identity,	represent,	all pu	compare	malcooms	SET PLA	COGNITICAN

Multiple	h bne s	wida w	hole n	imhare
Mulupi		VILLE IN		

- Solve problems with perimeter and area
- Multiply and divide fractions and decimals
- Use all operations on integers
 - Analyze properties and measures with 2- and 3-D shapes
 - Use all operations on positive and negative fractions
- Solve problems with percent, ratio, rate, and proportion
 - Relate similar triangles with slope of a line

BTH

Module Overview



National Mathematics Advisory Panel

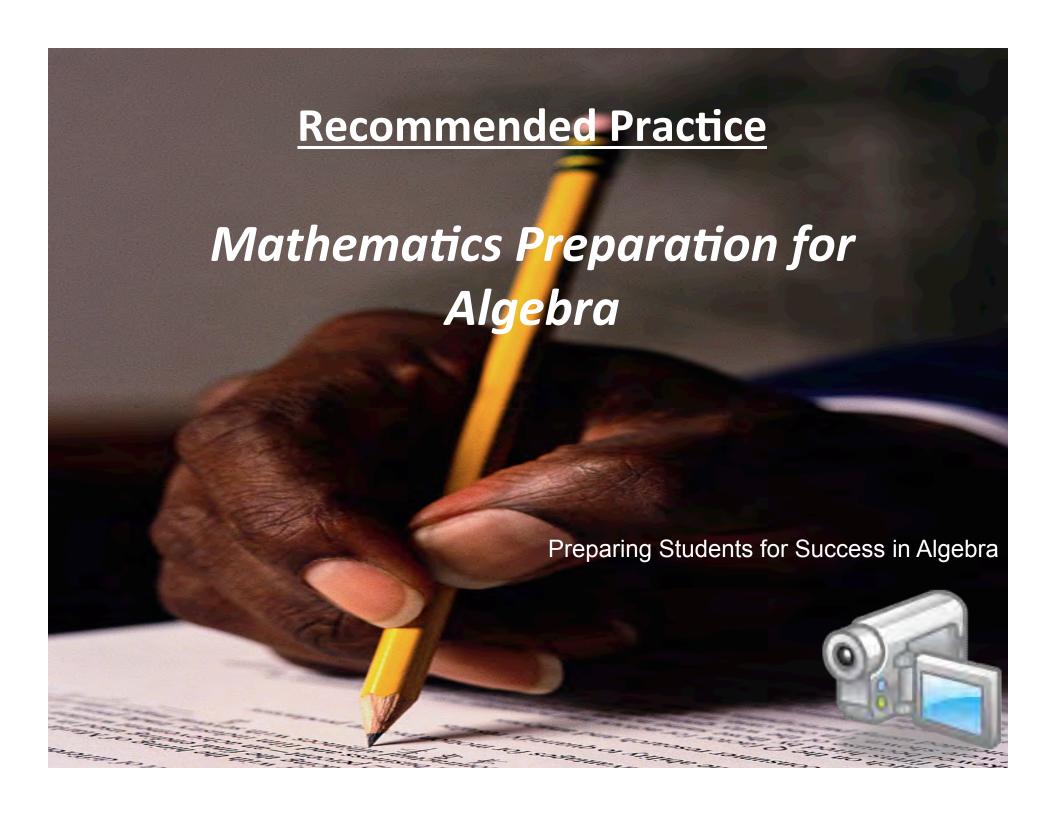


It's not just in Montana

Bradley Witzel from the Montana Reading Institute 2010



Montana educators identify by grade level topics students struggle with.





- Develop students' conceptual understanding and procedural knowledge of whole numbers, fractions, decimals, percents, and proportional reasoning and problem solving.
 - Classroom instruction must focus on the foundational topics of whole numbers and especially fractions. Students need to develop conceptual understanding and procedural knowledge to be successful at problem solving, and experience a mix of problem types and procedures to become proficient.





- Develop automatic recall of arithmetic facts, fluency with standard algorithms, and number sense.
 - Students must develop number sense and become fluent with whole numbers and fractions to be successful in mathematics. Teachers need to provide students with ample opportunities to develop automatic recall of facts, which provides a foundation for learning fractions, and competence with algorithms so they can solve problems quickly and efficiently.

- Build student understanding of the commutative, distributive, and associative properties and address topics of geometry and measurement that are relevant to algebra.
 - Along with developing fluency with whole numbers and fractions, students must be able to understand the commutative, distributive, and associative properties as they master the mathematical operations of addition, subtraction, multiplication, and division. Teachers should focus some part of instruction on geometry; in particular, similar triangles and measurement.



Learn What Works

Dr. Fennell

- The Critical Foundations
- Benchmarks as Guideposts
- Professional Development for the Critical Foundations



See How it Works

Focus on Key Topics

Number Sense

• Fractions, Decimals, Percents

Focus on Key Topics



MT K-12 Mathematics Content Standards

http://www.opi.mt.gov/pdf/Standards/10MathConStds.doc

- What are Montana's key topics?
- Pacing Guides for Pre-Algebra and Algebra I
 - Describe the features of a pacing guide.
 - How might a pacing guide be useful?



Number Sense

- The term "number sense" is a relatively new one in mathematics education. It is difficult to define precisely, but broadly speaking, it refers to "a well organized conceptual framework of number information that enables a person to understand numbers and number relationships and to solve mathematical problems that are not bound by traditional algorithms" (Bobis, 1996).
- The National Council of Teachers identified five components that characterize number sense: number meaning, number relationships, number magnitude, operations involving numbers and referents for numbers and quantities. These skills are considered important because they contribute to general intuitions about numbers and lay the foundation for more advanced skills.

Number Sense



3rd Grade Word Problem Example

Differentiated Student Assignments

- •How does the teacher prepare his students?
- •What type of learning environment is he using in this lesson?
- How are students demonstrating their understanding?

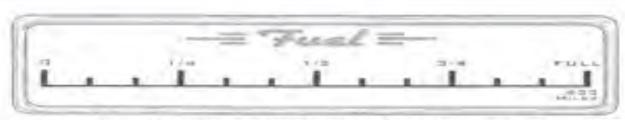


Differentiated Student Assignments

- Discussion/Write:
 - How could assignments like this be used in your classroom/school?
 - What preparation would you need to do in order for this to be successful?
 - What is the role of the teacher during an assignment like the example?
 - What might some barriers be to teachers using similar assignments?

Fractions, Decimals, Percents

- Expert Interview: Dr. Wu: Teaching Fractions
 - Reflect how you currently teach fractions and how Dr. Wu is describing the teaching of fractions.
- Using Multiple Representations to Teach Fractions
 - Keep track of those described in the video



Frank runs a business called Frank's Fresh Farm Produce. Once a week he drives north of the city to farms where he buys the best possible produce for his customers. Frank can travel 600 miles on a full tank of gas. His truck has a fancy, accurate fuel gauge.

Usually Frank has time to visit only one farm on each trip, but this week he decides to visit both Stan's and Louisa's farms. When Frank drives from his store to Stan's farm and back, he knows he uses 5/12 of a tank of gas. When he drives to Louisa's farm and back, he uses 1/3 of a tank of gas. From an area map, he learns that there is a road from Stan's farm to Louisa's farm that is 120 miles long. He realizes that he can drive from his store to Stan's farm, then to Louisa's farm, and then back to his store in one loop.

Frank can tell by looking at his fuel gauge that he has 5/8 of a tank of gas. Can he drive this loop without having to stop for fuel? Or, should he buy gas before he starts his trip?

Using a Number Line

 Bradley Witzel from the Montana Reading Institute 2010



 What background knowledge would a student would need to have in order to successfully solve these problems?

 What math skills would be necessary to use to solve these problems?



Do What Works

- Review current standards against NMP benchmarks.
- Learning Together About Mathematics Preparation for Algebra
- Planning Template #3: Working With Schools

Montana K-12 Mathematics Content Standards

http://www.opi.mt.gov/pdf/Standards/ 10MathConStds.doc







- Simultaneously develop students' conceptual understanding, procedural fluency, and problem-solving skills.
 - Mathematics instruction should focus on teaching conceptual understanding of mathematical operations, proficiency with operational procedures, and fluency with basic number facts all together, as each facilitates and reinforces learning in the others and they jointly support effective and efficient problem solving.



- Provide adequate practice opportunities to develop fluency with arithmetic facts and standard algorithms.
 - Teachers should provide practice that is distributed over time and includes a conceptually rich and varied mix of problems to help students develop fluency with facts and proficiency in operations, conceptual understanding, and problem solving.

Learn What Works

- Dr. Ferrini-Mundy
 - Lesson focus
 - Computational Fluency
 - Conceptual Understanding
 - Problem-Solving
 - What can schools do?
 - What about student motivation and the teacher's role in student motivation?



See How it Works

 Conceptual and Procedural Understanding

Effort and Persistence



Conceptual and Procedural Understanding

- Why is it important to develop students understanding of number sense while at the same time developing fluency with facts?
 - An Administrator's Perspective on Mathematics Instruction
- How can we fit it ALL in?
 - Specialist Teachers Provide Practice in Mathematics

Effort and Persistence

It matters!



 We need to have a plan to support and build on effort, stamina, and persistency



- What can I do to help struggling students persist when trying to solve problems?
- How can teachers reflect on our own teaching strategies to ensure that we are consistent in our communication about effort and practice?
- How can we work with other teachers in our schools to strengthen elements of the school culture that will support persistence?

Do What Works





- Establish benchmarks based on the Critical Foundations for Algebra to systematically gain mastery of key topics.
 - District and school benchmarks, curriculum, and assessments should be aligned with the benchmarks for the critical foundations and mastery points recommended by the National Mathematics Advisory Panel to ensure that instruction focuses on essential skills and topics and student learning proceeds at an effective pace.



Regularly use formative assessments to target and differentiate instruction.

Teachers should use formative assessment on a regular basis to monitor progress for all students and systematically examine assessment results to determine which groups of students should receive what types of interventions and to differentiate instruction for individuals needing more help with concept and skill development. For struggling students, formative assessment should be used once or twice a week.





Use a combination of instructional methods for students experiencing mathematical difficulties, including explicit instruction, multiple representations, and additional materials



Regular, explicit methods of instruction help students in the performance of computations, solving word problems, and solving problems that require the application of mathematics to novel situations.

This time should be dedicated to ensuring that students possess the foundational skills and conceptual knowledge necessary for understanding the mathematics they are learning at their grade level.



Differentiate instruction for mathematically gifted students.

Schools need to support appropriately challenging work in mathematics for gifted and talented students. Gifted students need a curriculum that is differentiated (by level, complexity, breadth, and depth), developmentally appropriate, and conducted at a more rapid rate. A mathematics program that includes a combination of acceleration and enrichment components is recommended.



Learn What Works

Use a mastery framework to guide instructional planning and student assessment

Expert Interview: Dr. Fuchs





Learn What Works

Dr. Fuchs: Research-Based Instructional

Programs

Design Features

- Explicitness
- 2. Instructional Design
- 3. Conceptually Rich
- 4. Drill and Practice
- 5. Cumulative Review
- 6. Motivating Instruction

See How it Works

- Benchmarks for Mastery
- Formative Assessments

Working with <u>All</u> Students:
 Struggling and Accelerated







The National Mathematics Advisory Panel report offers recommendations for how we can best prepare elementary and middle school students for success in algebra, a gateway to mathematics in high school and beyond.

Mathematics Preparation for Algebra

- -Follow a focused, coherent progression of mather
- Benchmarks for Mastery
 See How it Works:

Comprehensive Instruction

- Develop conceptual understanding, computational fluency, and problem-solving skills
- -Achieve automaticity in computation
- -Provide adequate practice
- Encourage effort and persistence

Mastery Framework

- —Set benchmarks for key skills
- —Use formative assessments
- Provide explicit instruction for struggling students
- -Offer acceleration and enrichment for gifted students



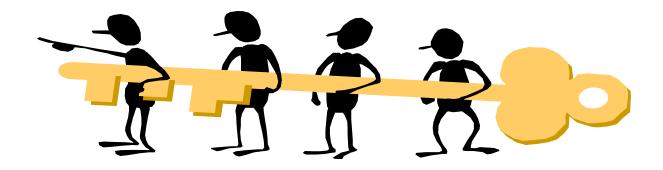
Grade-Level Benchmarks for Critical Foundations*

- 4TH I Identify, represent, and compare fractions and decimals
- Multiply and divide whole numbers
- Compare, add, and subtract fractions and decimals
 - Solve problems with perimeter and area
 - Multiply and divide fractions and decimals
 - Use all operations on integers
 - Analyze properties and measures with 2- and 3-D shapes
 - Use all operations on positive and negative fractions
- Solve problems with percent, ratio, rate, and proportion
 - Relate similar triangles with slope of a line





See How it Works ...Formative Assessments



- Reviewing student work
 - Protocols for Reviewing Student Work



- Formative Assessment on a Daily Basis
 - Six Elements of an Effective Math Lesson

See How it Works Working with All Students

Interventions for Struggling Students transcript

 Acceleration for Mathematically Gifted Students transcript



Do What Works

The Components of a Mastery Framework

 A checklist to aid staff to <u>understand</u> the key components of a mastery framework and to <u>assess</u> their school's progress toward implementing these components.



The Components of a Mastery Framework

Discuss in your teams:

- Which components are in place?
- Which components are partially in place?
- Which components are not at all in place?

- What are our priorities?
- Who are the persons responsible?



Do What Works

- Working with Struggling Students
 - Self-Assessment Inventory
 - This tool has been designed to help teachers identify whether or not they are implementing all the practices that might help students who are struggling in mathematics.



	Classroom Instruction	
1.	In each lesson I demonstrate to students how to solve problems.	Step-by-step modeling Think-alouds (sharing how I address a problem) Demonstrating more than one way to address a problem Explicit directions and explanations
2.	I demonstrate multiple examples of similar problems.	Examples that are similar Examples with slight variations Alternating challenging problems with easier problems
3.	I use multiple representations in demonstrations.	Concrete materials Representational materials Story contexts Visual diagrams Virtual demonstrations (via computer) Number line

Instruction: What might you add to your instruction or do more frequently to provide clearer instruction to students who are struggling?

		Student Practice		
1.	I encourage students to think aloud while solving problems.	Explain work to teacher Document steps taken in problem solving Using drawing or models to represent thinking Write about their work		
2.	I provide many opportunities for practice.	Guided practice (students work a problem and apchecked) In-class independent practice (support available) Worked examples are included for independent problem.	ble)	
3.	I encourage students to explain their solutions to other of Public Instruction Denise Juneau, State Superintendent	Working with a partner Working in cooperative groups Demonstrating worked solutions to class		



Do What Works

- Working with Mathematically Gifted Students
 - This tool has been designed to help school mathematics leaders and teachers to reflect about how well they are implementing practices to engage and challenge students who are gifted in mathematics.





Do What Works—Planning Template

- What does your school have in place?
- What does your school need to put into implementation?
- How do we prioritize the needs and who will be involved (roles/ responsibilities)?
- What is our timeline for the action plan items?





National Mathematics Advisory Panel

 "For all content areas, practice allows students to achieve automaticity of basic skills...which frees up working memory for more complex aspects of problem solving."

 "Students learn by building on prior knowledge, extending as far back as childhood."

References/Resources

- Doing What Works: http://dww.ed.gov/
- National Mathematics Advisory Panel Final Report: http://www2.ed.gov/about/bdscomm/list/mathpanel/report/final-report.pdf
- Montana Office of Public Instruction Rtl http://opi.mt.gov/Resources/RTI/ Index.html#gpm1 2
- Montana Office of Public Instruction Content Standards: http://www.opi.mt.gov/Curriculum/ Index.html